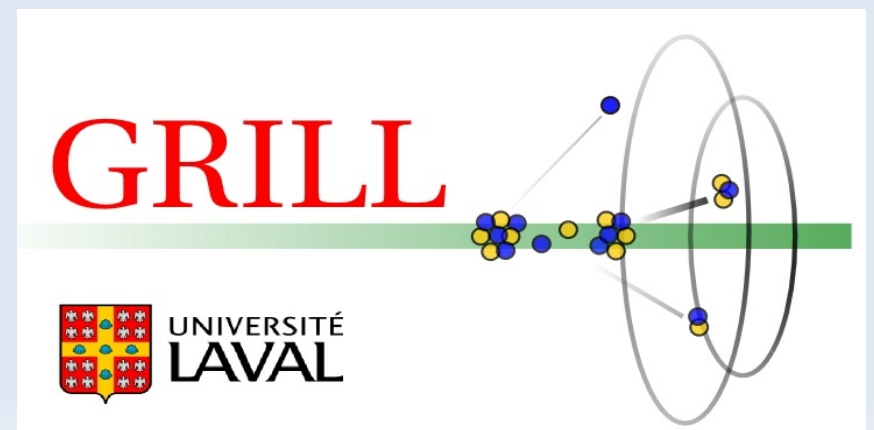


# Antisymmetrized Molecular Dynamics Calculations for Heavy-Ion Collisions

Patrick St-Onge  
Université Laval

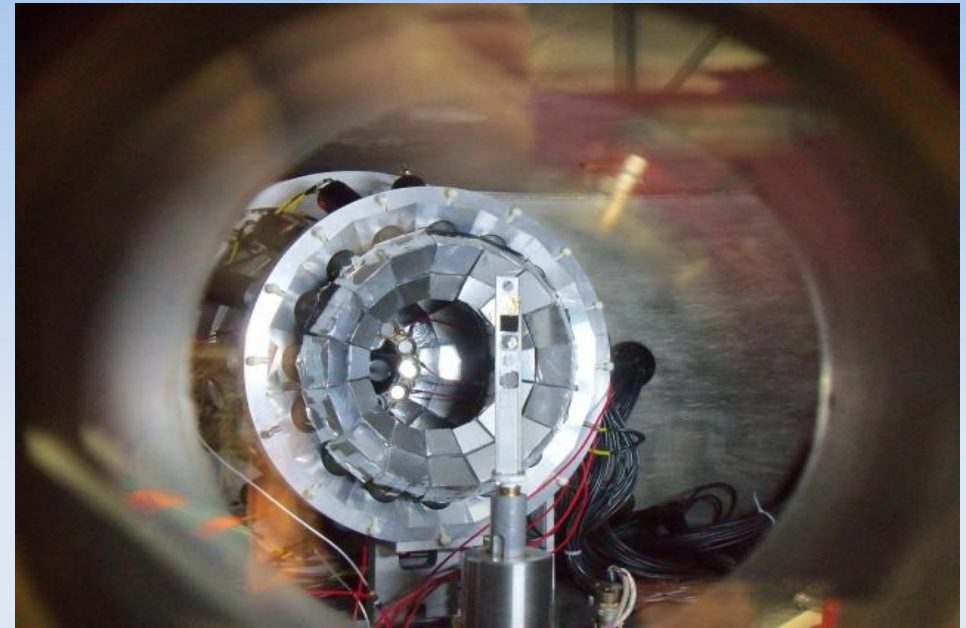


- Introduction and motivation
- Antisymmetrized Molecular Dynamics (AMD)
- Preliminary results
- Conclusion

# Introduction and motivation

- Heavy-Ion collisions at intermediate energies using the multidetector HERACLES
- Why intermediate energies?
  - 5-200 AMeV
  - Phase transition liquid-gas
    - Multifragmentation (IMF with  $Z > 2$ )
  - Transition between low energies and relativistic energies
    - Competing mechanisms
      - Mean field -Stochastic collisions
  - Nucleonic dynamics

- HERACLES description
- See Jérôme Gauthier presentation for more details



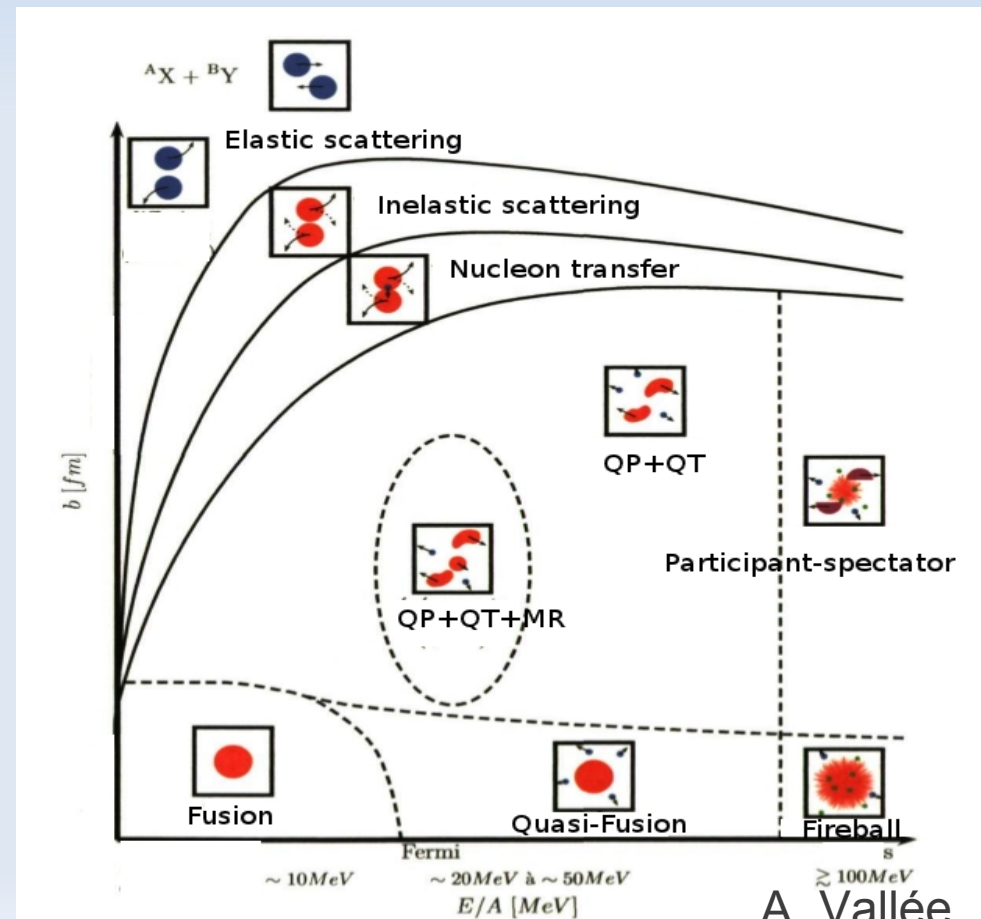
| Ring No. | $\Delta E$ detector | E detector       | $\theta_{min}$ ( $^{\circ}$ ) | $\theta_{max}$ ( $^{\circ}$ ) | N  | $\Delta\phi$ ( $^{\circ}$ ) | $\Delta E$ thickness ( $\mu\text{m}$ ) |
|----------|---------------------|------------------|-------------------------------|-------------------------------|----|-----------------------------|--|
| 0        | BC408               | BaF <sub>2</sub> | 4.8                           | 6                             | 6  | 15                          | 100                                    |
| 1        | Si                  | CsI(Tl)          | 6                             | 10                            | 8  | 18                          | 50                                     |
| 2        | BC408               | BC444            | 10.5                          | 16                            | 16 | 22.5                        | 100                                    |
| 3        | BC408               | BC444            | 16                            | 24                            | 16 | 22.5                        | 100                                    |
| 4        | -                   | CsI(Tl)          | 24                            | 34                            | 16 | 22.5                        | -                                      |
| 5        | -                   | CsI(Tl)          | 34                            | 46                            | 16 | 22.5                        | -                                      |

- Dynamic of heavy-ion collisions at intermediate energies

QP=Quasi-Projectile

QT=Quasi-Target

MR=Mid-Rapidity



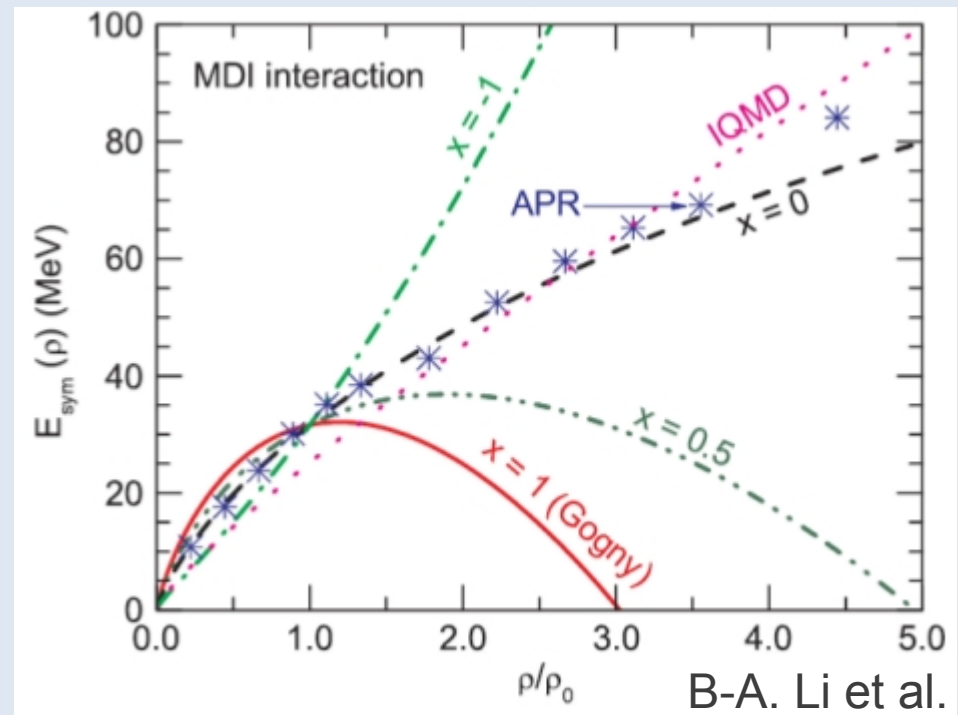
- Equation of state (EOS)

- $E(\rho, \delta) = E(\rho, \delta=0) + E_{\text{sym}}(\rho) \cdot \delta^2 + \dots$

$$\delta = (\rho_n - \rho_p) / \rho$$

$\rho_n$  = neutron density

$\rho_p$  = proton density



- TRIUMF ISAC-II Rare-Isotope beams
  - Rare-Isotope beams are available up to 15 AMeV
- July 2011 experiment
  - $^{25}\text{Na}+^{12}\text{C}$  at 9.23 AMeV     $N/Z=1.27$
  - $^{25}\text{Mg}+^{12}\text{C}$  at 9.23 AMeV     $N/Z=1.08$

# AMD

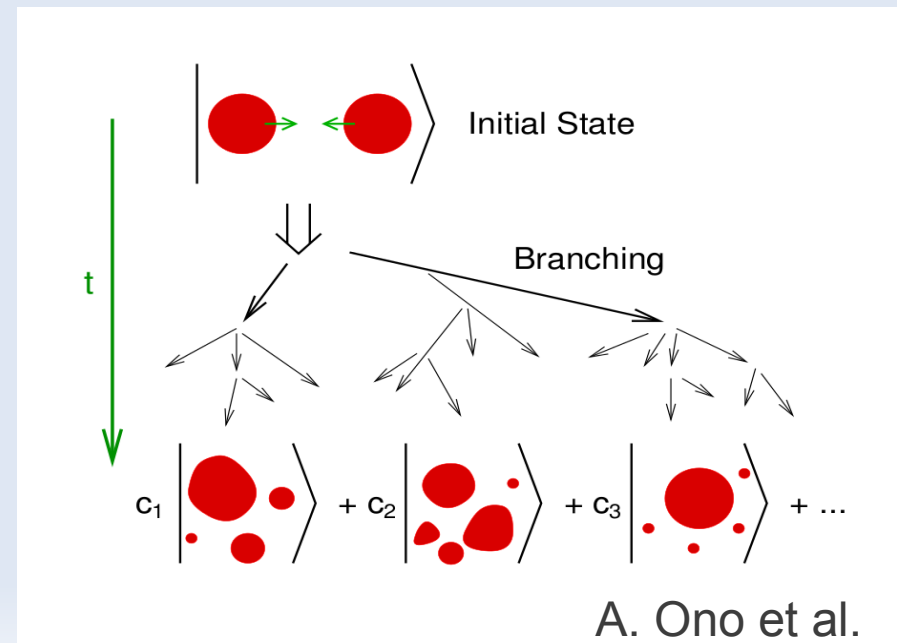
- Transport models
  - Microscopic one-body
    - Time-Dependent Hartree-Fock (TDHF)
      - Mean field only
      - Difficulty to produce fragments distribution and fusion at intermediate energy
    - Boltzmann-Uehling-Uhlenbeck (BUU)
      - Mean field and NN collision
      - Not applicable below 10-15 AMeV



- Microscopic N-body
  - Classic molecular dynamics
    - Follow motion of N body using the Hamiltonian
    - Don't respect Pauli principle
  - Quantum molecular dynamics (QMD)
    - Respect Pauli principle using BUU-type two-body collisions
  - Antisymmetrized molecular dynamics (AMD)
    - Build to respect Pauli principle

- AMD details

- Nucleon are represented by wave packet with fixed width
- Antisymmetrization of wave functions
- A stochastic BUU-type NN collision algorithm is used
- Quantum Branching



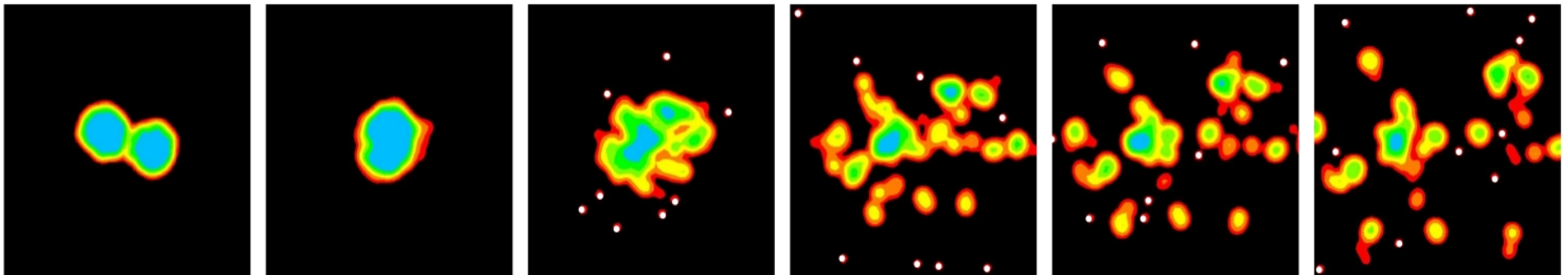
- AMD wave function and stochastic equation of motion

$$|\Phi(Z)\rangle = \det_{ij} \left[ \exp \left\{ -\nu \left( r_j - \frac{Z_i}{\sqrt{\nu}} \right)^2 \right\} \chi_{\alpha_i}(j) \right] |\varphi\rangle$$

$$Z_i = \sqrt{\nu} D_i + \frac{i}{2\hbar\sqrt{\nu}} K_i$$

$$\frac{d}{dt} Z_i = \{Z_i, H\} + \Delta Z_i(t) + (NN \text{ collisions})$$

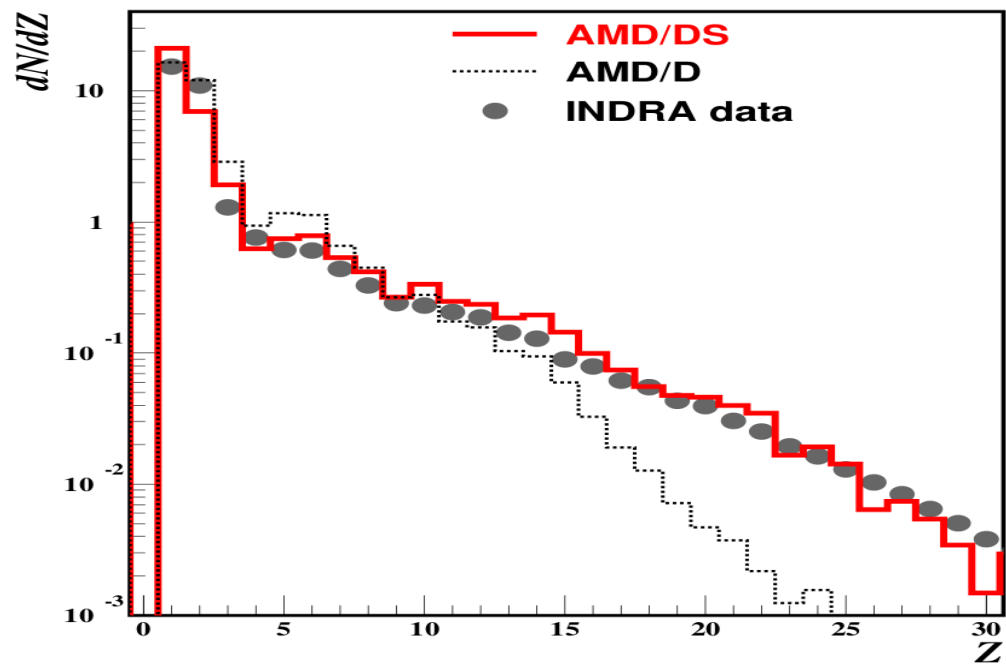
- Schematic time evolution of a Xe + Sn at 50 AMeV reaction simulated by AMD



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- AMD results compared with INDRA data for Xe + Sn at 50 AMeV

## Charge distribution

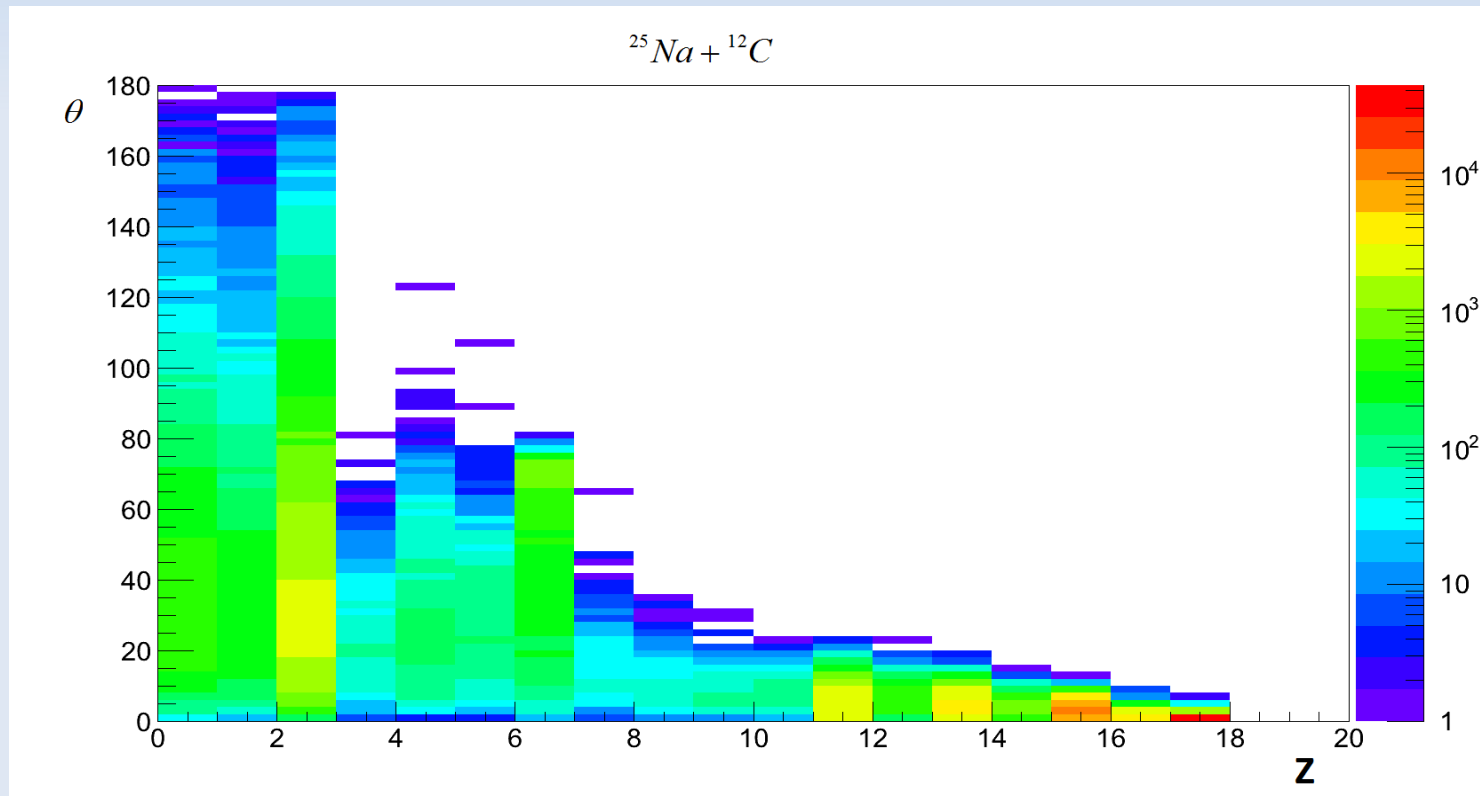


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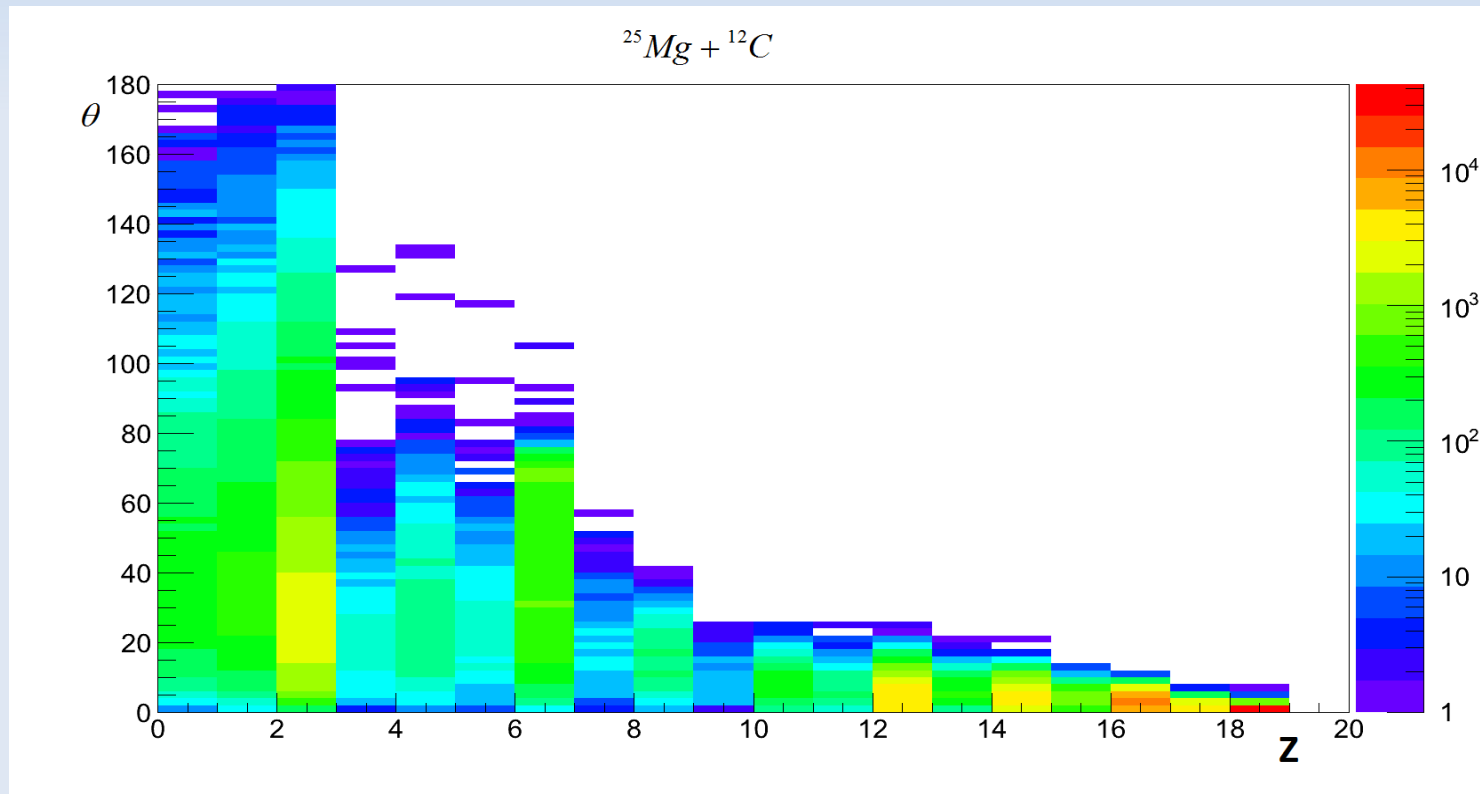
# Preliminary Results

- Simulation summary
  - 115 000 events simulated for  $^{25}\text{Na} + ^{12}\text{C}$  and  $^{25}\text{Mg} + ^{12}\text{C}$  at 9.23 AMeV
  - Impact parameter  $0 < b < 7$  (fm)
  - Freeze-out at  $t=300$  fm/c and  $dt=0.75$  fm/c
  - Standard Gogny interaction
  - 24 hours of compute time on 320 cores (Colosse)

- Fragments distribution at freeze-out  $t=300$  fm/c  
 $^{25}\text{Na} + ^{12}\text{C}$  at 9.23 A MeV

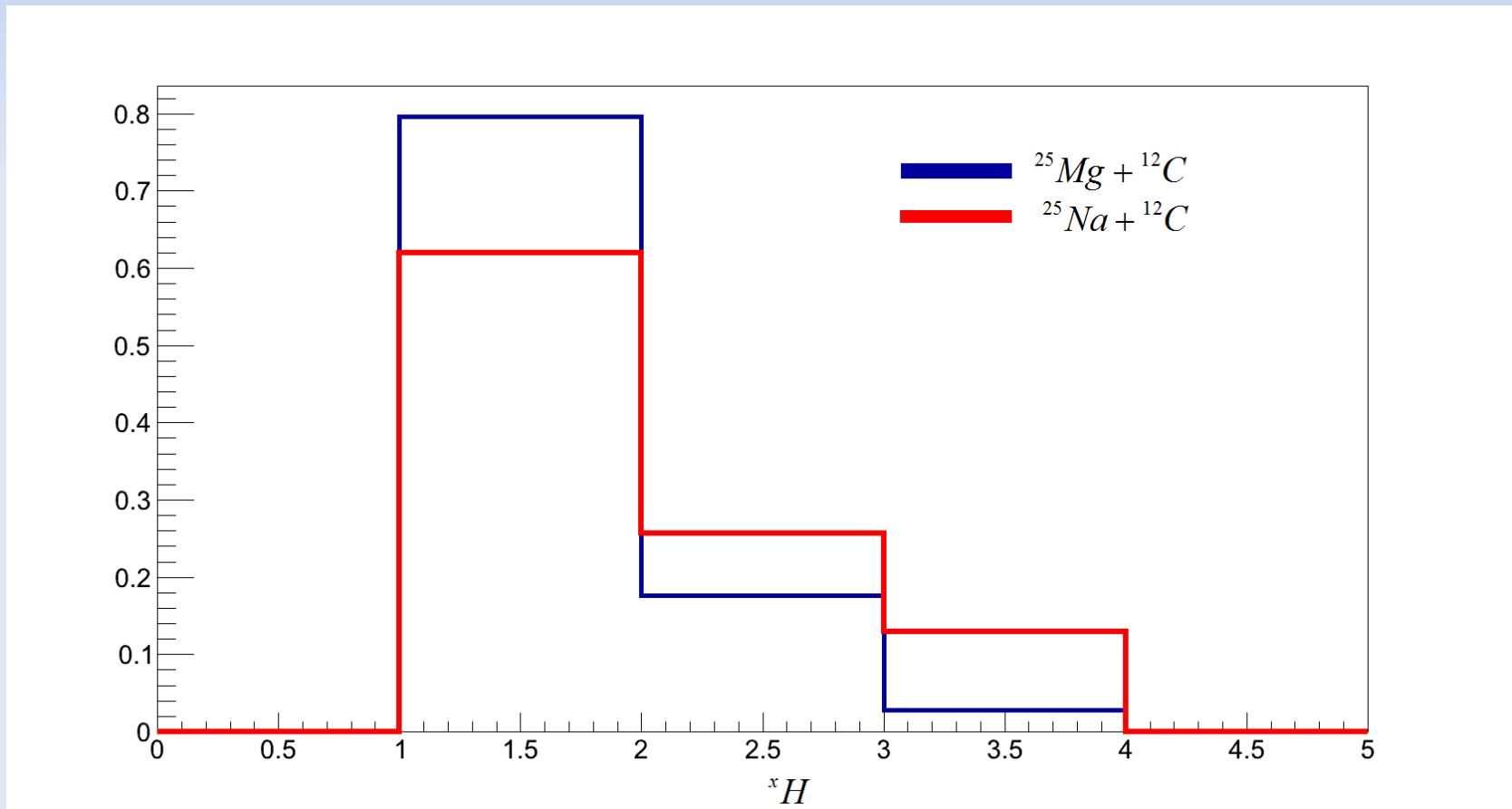


- Fragments distribution at freeze-out  $t=300$  fm/c  
 $^{25}\text{Mg} + ^{12}\text{C}$  at 9.23 AMeV

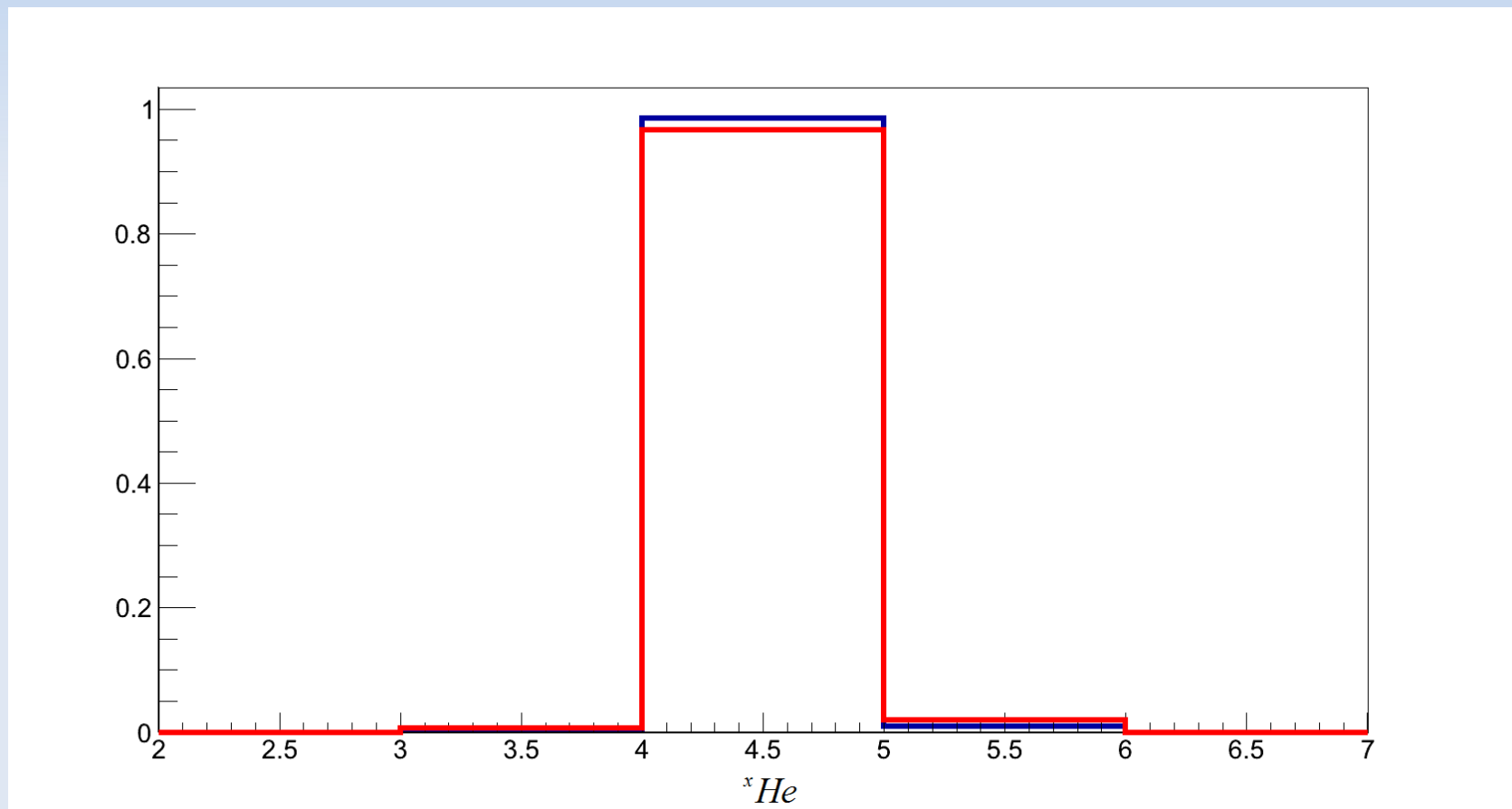




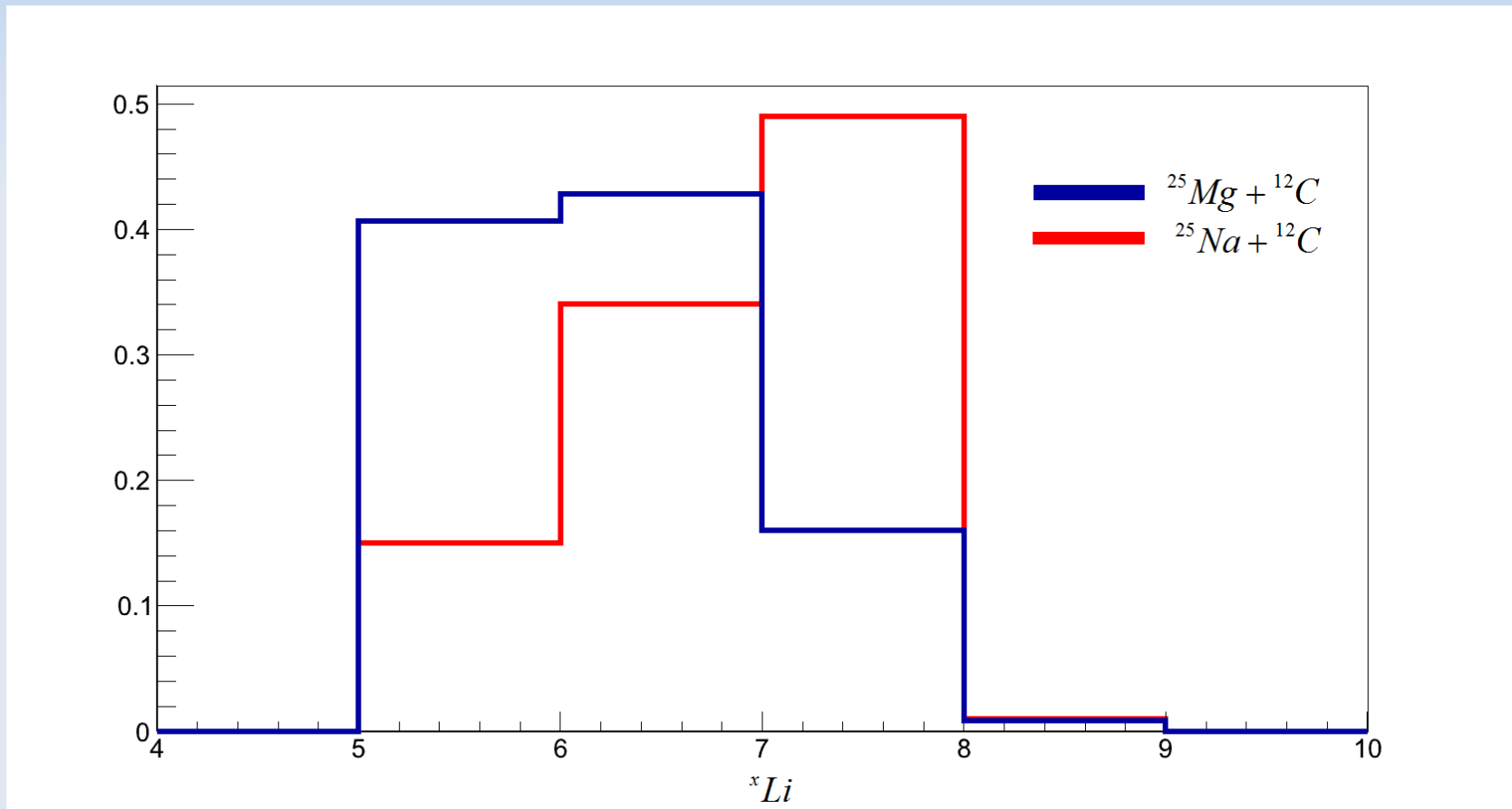
- Isotope distributions at  $t=300$  fm/c - H



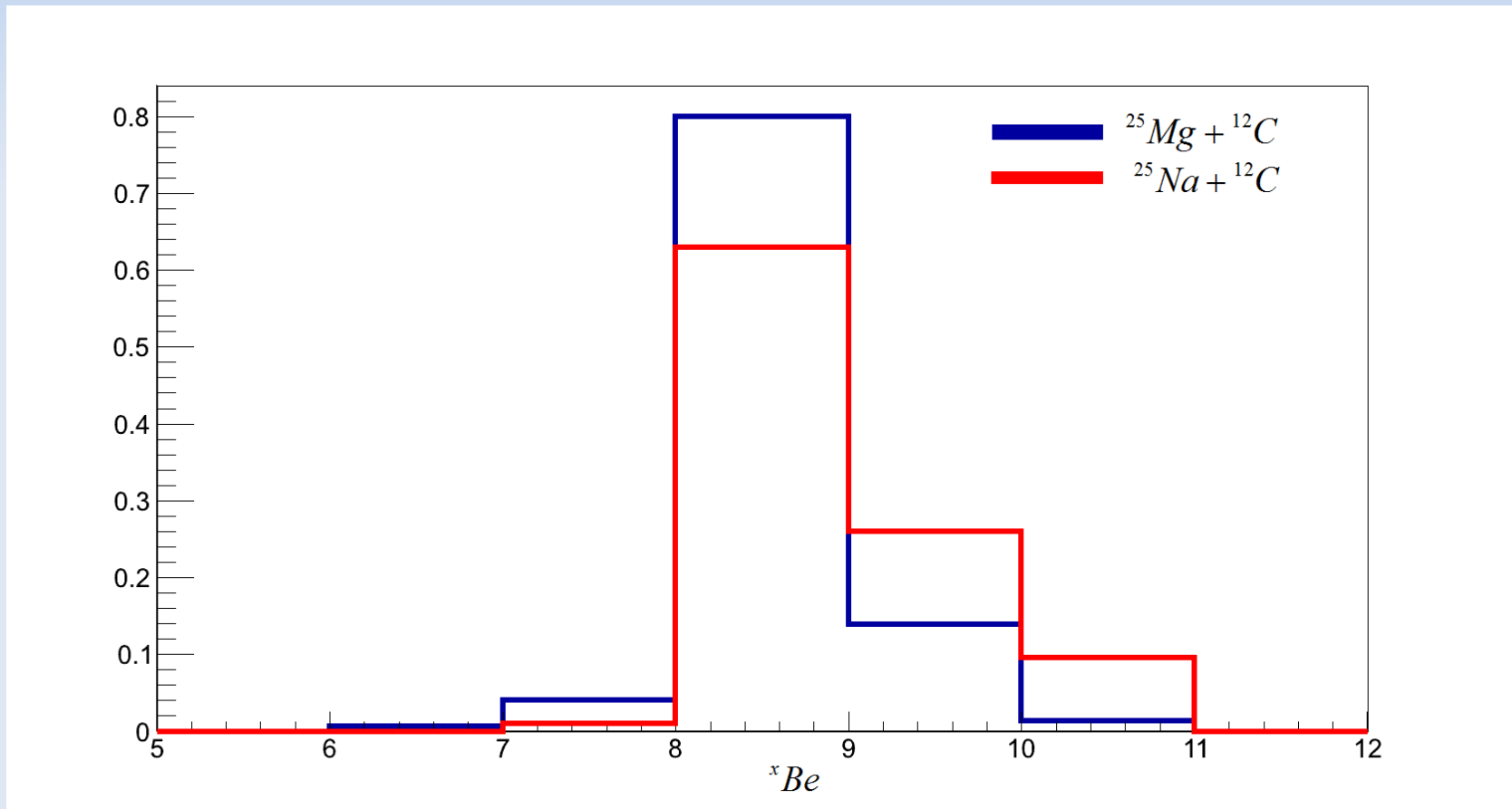
- Isotope distributions at  $t=300$  fm/c - He



- Isotope distributions at  $t=300$  fm/c - Li



- Isotope distributions at  $t=300$  fm/c - Be



# Conclusion

- Still a lot of work to do
  - Statistical decay of fragments
  - Test other interactions (Skyrme, Gogny-As)
  - Compare with experimental data
- Identification and calibration is already done on experimental data