## PHYSICS 198-620B

## Experimental Techniques in Sub-Atomic Physics

## CALORIMETRY ASSIGNMENTS

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deadline: March  $25^{th}$ , 2009, 11 am legible handwriting!

- 1. (50%) For an incoming electron of energy  $E_0$ , develop a simple shower model where, on an average path  $\chi_0$  (the radiation length), every electron of the cascade always radiates half of its energy to bremsstrahlung and every photon of the cascade always makes pair production until the particles reach the known critical energy  $E_c$ . Only at this point would all energies be released into ionization processes and/or be dissipated.
  - (a) Find the depth at which this occurs.
  - (b) Find the number of particles involved in the whole shower process.
  - (c) Find the total track length for charged particles in units of  $\chi_0$ .
  - (d) Estimate what would be the duration time of a 1 GeV  $e^-$  shower in lead.
- 2. (50%) Imagine a wall made of a large assembly of BGO crystals. Their front faces are squares with sides equal to a Moliere radius. Given "d" as the perpendicular distance to a source of energetic  $\pi^{0}$ 's,
  - (a) Define your own rough criterium for "d" to resolve with high probability (e.g. better than 68%) the two most probable decay products, i.e. identify the  $\pi^{0}$ 's.
  - (b) For a wide range of  $\pi^0$  momenta (one value per order of magnitude, e.g. 0.01 GeV, 0.1 GeV, 1 GeV, etc.. as long as a detector size might make sense):
    - i. Calculate the average decay length in the laboratory.
    - ii. Calculate the minimum distance "d" where the wall detector should be to perform  $\pi^0$  identification according to your criterium. Can the decay lengths be neglected?